Noise Reduction for Wideband Speech Exploiting Spectral Dependencies Based on Conditional Estimation

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Abstract

This contribution presents a wideband (50 Hz - 7 kHz) speech enhancement system that is operating in the frequency domain. A conventional noise suppression is used in the low band, while a joint noise suppression approach is applied in the high band using techniques known from artificial bandwidth extension (BWE). Statistical dependencies between the low band (50 Hz - 4 kHz) and the high band (4-7 kHz) are exploited. Features from the processed (enhanced) low band signal are extracted and used to estimate subband energies of the high band. The weighting gains determined from these energy estimates are adaptively combined with conventional gains obtained in addition for the high band. As novel feature compared to [1] the BWE training process incorporates noisy speech and more appropriate features resulting in a better noise estimate. The performance of the proposed method is shown to be consistently better than the conventional approach and [1].

1 Introduction

The acoustic bandwidth in telephony systems is typically limited to the frequency range between 300 Hz and 3.4 kHz. However, this typical "telephone sound" cannot satisfy the increased demands as the perceived speech quality is considerably reduced compared to the full audio bandwidth. As a reasonable compromise, various wideband (50 Hz - 7 kHz) speech codecs have been developed in the past (e.g., the Adaptive Multi-Rate (AMR) Wideband Codec [2]) and are about to be introduced in current mobile networks. Nevertheless, most of these codecs are mainly designed for nearly noise-free input speech signals and do not perform well when the input signal is degraded by acoustic background noise. In order to improve the listening comfort and to keep the high quality also in noisy environments, noise suppression techniques are required for wideband communication systems.

One of the popular methods for enhancing degraded speech represents the noisy speech in the short-time Fourier domain and applies individual adaptive gains to each frequency bin. Most of the rules proposed in liter-ature have been derived for low band (50 Hz - 4 kHz) signals under certain assumptions about the statistics of the speech and noise signals, e.g., [3, 4, 5]. When it comes to wideband noise reduction, an established method is to double sampling rate and transform length and to apply the low band algorithms also for the wider frequency band. Thereby, neither the unequal spectral energy distribution of speech and noise signals nor the properties of the human auditory system are considered.

For a wide range of realistic noise sources, it can be shown that the signal-to-noise ratio (SNR) significantly degrades beyond 4 kHz leading to imprecise noise reduction and fluctuating weighting gains that result in the increased occurrence of *musical noise* especially at higher frequencies.

It is known that the spectral dependencies of speech

signals can be exploited to estimate missing high frequency components by utilizing only the low band speech signal. This technique, called artificial bandwidth extension (BWE) (e.g., [6], [7]), aims at increasing the perceived speech quality if only the low band signal is available. In this paper, wideband speech enhancement is combined with artificial BWE techniques. While a conventional noise suppression technique is used in the low band, a joint approach is applied for the speech enhancement in the high band (4-7 kHz). Based on a trained hidden Markov model (HMM), features from the processed (enhanced) low band signal are extracted and used to estimate subband energies of the high band speech signal. The resulting weighting gains determined from these energy estimates are adaptively combined with conventional gains for the high band. Compared to [1] the BWE training process incorporates noisy speech. Additionally more appropriate features are extracted from the low band which minimize speaker differences and short-term noise variations.

The remainder of this paper is organized as follows: In Sec. 2, a brief overview of the proposed system is given. Sec. 3 comprises the procedure of the combined noise suppression in the high band in detail. Experimental results are shown in Sec. 4 and conclusions are drawn in Sec. 5.

2 System Overview

A simplified block diagram of the proposed wideband speech enhancement system is depicted in Fig. 1. It is assumed that the noisy input signal y(k) consists of the clean speech signal s(k) which is degraded by an additive noise signal n(k) according to:

$$y(k) = s(k) + n(k), \tag{1}$$

where k is the discrete time index. Different processing schemes are applied in the low band (50 Hz-4 kHz) and the high band (4-7 kHz). Therefore, a 2-channel infinite impulse response (IIR) quadrature mirror filter (QMF) bank with critical sampling and near perfect reconstruction [8] is used to split the wideband signal y(k) into the low band and the high band signal. Due to the decomposition, individual analysis-synthesis structures and different algorithms can be used in each band enabling the re-use of existing low band noise reduction systems. After downsampling the lowpass and highpass filtered signals by a factor of 2, a conventional noise reduction technique is applied to the low band signal $y_{\text{lb}}(k')$ where k' represents the discrete time index in the subsampled domain.



Figure 1: Wideband noise reduction using different techniques in low band and high band exploiting spectral dependencies.



Figure 2: High band noise reduction exploiting spectral dependencies between low band and high band.

In the high band, the noisy signal $y_{hb}(k')$ is enhanced by using additional information from the improved low band signal. For this, features from the vector \tilde{S}_{lb} , consisting of the spectral coefficients from the processed low band signal, are extracted. In both bands, the noise suppression is performed in the frequency domain. Therefore, $y_{xx}(k')$ is segmented into overlapping frames of length L_F , where the index 'xx' denotes either the low band 'lb' or the high band 'hb'. After windowing and zero-padding, the fast Fourier transform (FFT) of length M_F is applied to these frames. Hence, the spectral coefficients of the noisy input signal at frequency bin μ and frame λ are given by:

$$Y_{\rm xx}(\lambda,\mu) = S_{\rm xx}(\lambda,\mu) + N_{\rm xx}(\lambda,\mu), \qquad (2)$$

where $S_{xx}(\lambda, \mu)$ and $N_{xx}(\lambda, \mu)$ represent the spectral coefficients of the speech and the noise signal

In the low band noise suppression is achieved by spectral weighting: $\hat{S}_{\rm lb}(\lambda,\mu) = Y_{\rm lb}(\lambda,\mu) \cdot G_{\rm lb}(\lambda,\mu)$. Limiting the weighting gains $G(\lambda,\mu)$ to a lower bound $\max(G(\lambda,\mu),g_{\rm min})$ prevents speech distortion at the expense of noise attenuation. The favored tradeoff between noise attenuation and speech distortion depends on the application. While for the performance of the BWE stronger noise attenuation (using a small $\tilde{g}_{\rm min}$) is desirable, a reasonable amount of speech distortion in the enhanced low band signal $\hat{s}_{\rm lb}(k')$ is obtained by using a higher $g_{\rm min}$. The respective enhanced signals $\hat{s}_{\rm lb}(k')$ and $\hat{s}_{\rm hb}(k')$ are upsampled and lowpass and highpass filtered again. Finally, both signals are combined by a QMF synthesis in order to obtain the enhanced wideband signal $\hat{s}(k)$.

3 Joint Noise Reduction in the High Band

The main energy of a speech signal is usually located in the frequency range between 500 Hz and 3 kHz. Mostly the energy of speech signals declines stronger than the energy of noise signals beyond 3 kHz, hence the SNR in the low band is higher than in the high band. Table 1 shows some quantitative examples of how much the SNR in the low band is better than in the high band for different speakers and different noise environments. It can be seen that in most cases the SNR significantly degrades in the high band which leads to imprecise noise reduction and fluctuating weighting gains resulting in the increased occurrence of musical tones especially at higher frequencies. So far, only a very limited number of proposals have been made which take into account the aforementioned aspects when enhancing wideband speech signals, e.g., [1] and [9]. To counteract this problem, a joint noise reduction method based on [1] is presented in this paper for the high band signal which makes use of the spectral dependencies between low band and high band.

Noise Type	Average Ratio of Low Band SNR and High Band SNR for		
	Male Speakers	Female Speakers	
Cockpit Babble Factory Buccaneer WGN	+15.39 dB +0.55 dB +12.55 dB +15.64 dB +26.81 dB	+13.98 dB -0.86 dB +11.14 dB +14.23 dB +25.39 dB	

Table 1: SNR deviation of the low band from the high band for different noise types. For the measurement, six speech signals (three male and three female speakers) from the NTT database were used. The noise signals have been taken from the NOISEX-92 database.

Figure 2 shows the basic principle of the combined noise reduction scheme in the high band. The FFT analysis and synthesis structure remains the same as for the low band signal. After the transformation into the frequency domain, two separate noise suppression methods are applied to the noisy high band spectrum $Y_{\rm hb}(\lambda)$ resulting in the calculation of the high band weighting gains $G_{\rm hb}(\mu')$ where μ' represents the subsampled frequency index as will be explained later.

As depicted in Fig. 2 two gain calculations are performed, resulting in conventional gains G_{conv} and new gains G_{bwe} for the high band. The conventional approach for the noise reduction consists of noise power estimation (e.g., [10]), SNR estimation (e.g., [10]) and the calculation of the weighting gains $G_{\text{conv}}(\mu)$ (e.g., [3, 4, 5]). A following post processing stage decreases the frequency resolution from M_F to M'_F ($M'_F < M_F$) by combining adjacent frequency-bins using overlapping Hann windows of the same length. The decimated frequency index is denoted by μ' . Therewith the properties of the human auditory system are taken into account, i.e. the frequency selectivity decreases with higher frequencies. In addition the variance of the weighting gains is reduced leading to a better suppression of musical tones.

In the upper branch of Fig. 2 artificial BWE techniques are used to determine the weighting gains G_{bwe} (see next section for details). All required processing steps are thereby performed at the reduced frequency resolution M'_{F} as well. The resulting weighting gains $G_{\text{bwe}}(\mu')$ are adaptively combined with $G_{\text{conv}}(\mu')$ according to:

$$G_{\rm hb}(\mu') = \alpha \cdot G_{\rm bwe}(\mu') + (1 - \alpha) (\mu') \cdot G_{\rm conv}(\mu'), \quad (3)$$

where $\alpha \in [0,1]$ represents a cross-fading factor that is frame and frequency dependent.

Finally, the frequency resolution of the high band weighting gains $G_{\rm hb}(\mu')$ is expanded (interpolated) back from $M'_{\rm F}$ to the original resolution $M_{\rm F}$ using overlap-add of scaled Hann windows. A spectral weighting of the noisy high band coefficients $Y_{\rm hb}(\mu)$ with the weighting gains

 $G_{\rm hb}(\mu)$ yields an estimate $\hat{S}_{\rm hb}(\mu)$ of the clean high band coefficients $S_{\rm hb}(\mu)$:

$$S_{\rm hb}(\mu) = Y_{\rm hb}(\mu) \cdot G_{\rm hb}(\mu). \tag{4}$$

An inverse fast Fourier transform (IFFT) and overlap-add is applied to obtain the enhanced signal $\hat{s}_{hb}(k')$ in the time domain.

3.1 Noise Reduction Exploiting Spectral Dependencies

In order to exploit the dependencies in the frequency domain between low band and high band, techniques known from artificial BWE are applied for the wideband noise reduction. The main principle that is used here for the BWE is partly included in [6]. The concept consists of estimating high band signal parameters based on features that are extracted only from the enhanced low band signal using a trained Hidden Markov Model (HMM). In a real application, the processed low band signal will either still contain remaining background noise or be distorted due to the noise suppression algorithm. In contrast to [1], where the HMM is trained with clean speech only, this fact is incorporated into the training process of the artificial BWE in this contribution. Therefore, the training data used to determine the features is degraded by white Gaussian noise with an SNR of 0 dB and processed with a conventional noise reduction system (e.g., [3, 4, 5]) using strong noise suppression (\tilde{g}_{\min}). Thus, typical processing artefacts are incoporated in the training process.

Usually, representations of the spectral envelope of the low band signal are used as features that are extracted on a frame-by-frame basis [11]. In [1] the used features consists of mel-frequency cepstral coefficients (MFCCs), while in this contribution the feature vector x from the low band consists of $N_{\rm C}$ Relative Spectral Transform - Perceptual Linear Prediction (RASTA-PLP) coefficients and the zero-crossing rate (ZCR) of the low band signal $\tilde{S}_{\rm lb}$. RASTA [12] is a technique that applies a filter in each frequency subband in order to smooth over short-term noise variations and to remove any constant offset resulting from static spectral coloration in the speech channel. The PLP [13] algorithm preserves the important speech information by warping spectra to minimize the differences between speakers.

According to [6], a trained HMM is used to estimate the feature vector \mathbf{v} , representing the M'_F subband energies of the high band signal. Let $\mathbf{X} = {\mathbf{x}(1), ..., \mathbf{x}(\lambda)}$ be a sequence of feature vectors from the low band of frames 1 to λ . The criterion for MMSE estimation of a vector \mathbf{v} , with given observations \mathbf{X} is $\mathscr{E}\{||\mathbf{v} - \hat{\mathbf{v}}||^2|\mathbf{X}\} = \min$, where $\hat{\mathbf{v}}$ is the respective estimate. The solution to this optimization problem is the conditional expectation $\mathbf{v}_{\text{MMSE}} = \mathscr{E}\{\mathbf{v}|\mathbf{X}\}$. Using a precomputed codebook $\mathscr{C} = {\hat{\mathbf{v}}_1, ..., \hat{\mathbf{v}}_{M_C}}$ for the vectors \mathbf{v} (e.g., obtained with the LBG algorithm [14]), this MMSE estimate can be expressed as [11, 7]:

$$\hat{\mathbf{v}}_{\text{MMSE}} = \sum_{\hat{\mathbf{v}}_i \in \mathscr{C}} \hat{\mathbf{v}}_i \cdot P(\hat{\mathbf{v}}_i | \mathbf{X}), \tag{5}$$

which essentially is a weighted sum over the $M_{\rm C}$ centroids of the codebook \mathscr{C} . Thereby, the weights $P(\hat{\mathbf{v}}_i | \mathbf{X})$ specify a posteriori probabilities which can be calculated using HMM techniques [6].

Once the instantaneous energies of the M'_F subbands $\hat{\mathbf{v}} = \{|\hat{S}_{hb}(0)|^2, ..., |\hat{S}_{hb}(M'_F - 1)|^2\}$ have been estimated, they are, in turn, used to estimate the noise power in the high band signal:

$$|\hat{N}_{\rm hb}(\mu')|^2 = \max\left(|Y_{\rm hb}(\mu')|^2 - |\hat{S}_{\rm hb}(\mu')|^2, 0\right), \quad (6)$$

with $0 \le \mu' \le M'_F - 1$. Finally, the *a posteriori* SNR $\gamma(\mu')$ and *a priori* SNR $\xi(\mu')$ can be estimated according to:

$$\hat{\gamma}_{\rm hb}(\mu') = \frac{|Y_{\rm hb}(\mu')|^2}{|\hat{N}_{\rm hb}(\mu')|^2} \quad \text{and} \quad \hat{\xi}_{\rm hb}(\mu') = \frac{|\hat{S}_{\rm hb}(\mu')|^2}{|\hat{N}_{\rm hb}(\mu')|^2}, \quad (7)$$

which are required in order to calculate the weighting gains $G_{\text{bwe}}(\mu')$ to be used in Eq. 3.

3.2 Cross-Fading Factor

It has already been mentioned that the two weighting gains $G_{\rm conv}(\mu')$ and $G_{\rm bwe}(\mu')$ are adaptively combined using the cross-fading factor $\alpha(\mu')$, see Eq. 3. In the following, the reference cross-fading factor $\alpha_{\rm ref}(\mu')$ is defined as:

$$\alpha_{\rm ref}(\mu') = \frac{\left(G_{\rm opt}(\mu') - G_{\rm conv}(\mu')\right)^2}{\left(G_{\rm opt}(\mu') - G_{\rm conv}(\mu')\right)^2 + \left(G_{\rm opt}(\mu') - G_{\rm bwe}(\mu')\right)^2}, \quad (8)$$

where $G_{opt}(\mu')$ represents the ideal weighting gain that could in theory (or by a dedicated simulation setup) be determined from the clean speech and noise signal according to the ideal *a posteriori* SNR $\gamma_{opt}^{hb}(\mu')$ and *a priori* SNR $\xi_{opt}^{hb}(\mu')$:

$$\gamma_{\text{opt}}^{\text{hb}}(\mu') = \frac{|Y_{\text{hb}}(\mu')|^2}{|N_{\text{hb}}(\mu')|^2} \quad \text{and} \quad \xi_{\text{opt}}^{\text{hb}}(\mu') = \frac{|S_{\text{hb}}(\mu')|^2}{|N_{\text{hb}}(\mu')|^2}, \quad (9)$$

which are also determined at the reduced frequency resolution $M'_{\rm F}$ by combining adjacent frequency bins as before. If the conventional noise suppression technique performs better than the BWE approach, i.e., $(G_{\rm opt} - G_{\rm conv})^2 < (G_{\rm opt} - G_{\rm bwe})^2$, $\alpha_{\rm ref}$ in Eq. 8 tends to smaller values leading to a stronger weighting of $G_{\rm conv}$ in Eq. 3 and vice versa.

In order to estimate the optimal cross-fading factor in a realistic scenario, first $\alpha_{ref}(\mu')$ is recorded in a training process for every frame λ and every subband μ' together with the respective subband SNR $\xi_{opt}^{hb}(\mu')$ of the high band and the averaged SNR $\bar{\xi}_{opt}^{lb}$ of the low band:

$$\bar{\xi}_{\rm opt}^{\rm lb} = \frac{1}{M_{\rm F}} \sum_{\mu=0}^{M_{\rm F}-1} \frac{|S_{\rm lb}(\mu)|^2}{|N_{\rm lb}(\mu)|^2}.$$
 (10)

Based on the training data, a look-up table for the estimation of $\alpha(\mu')$ is generated for every subband. Therefore, $\xi_{opt}^{hb}(\mu')$ and $\bar{\xi}_{opt}^{lb}$ are quantized (e.g., 1 dB step size) and the associated values for $\alpha_{ref}(\mu')$ are averaged within the quantization levels. At the end, the final look-up table provides one estimate $\bar{\alpha}(\mu')$ for each quantized combination of $\xi_{opt}^{hb}(\mu')$ and $\bar{\xi}_{opt}^{lb}$. In a real application, ξ_{opt}^{hb} and $\bar{\xi}_{opt}^{lb}$ are not available. Here, the respective SNR estimates of the conventional noise suppression techniques in the low band and high band are utilized to determine $\bar{\alpha}(\mu')$ using a pretrained look-up table.

4 Results

In principle, any noise reduction technique can be applied within the proposed system to perform the suppression in the low band and to estimate the conventional weighting gains G_{conv} in the high band. For the evaluation in this paper, the well-known Wiener filter [3] is used. In this investigation, the proposed noise suppression techniques with

Low and High Band: Wiener fil	ilter [3	3]
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Parameter	Settings
Sampling frequency	16 kHz
Frame length $L_{\rm F}$	160 (= 20 ms due to downsampling)
FFT length $M_{\rm F}$	256 (including zero-padding)
Frame overlap	50% (Hann window)
Input SNR	-10 dB 35 dB (step size: 5 dB)
Noise estimation	Minimum Statistics [10]
SNR estimation	Decision-directed approach [4]
Number subbands $M'_{\rm E}$	24
Number RASTA-PLPs N _C	13
Codebook size M_C	128 (training based on 1.5 h speech)
Gain limitation $(\tilde{g}_{\min} / \tilde{g}_{\min})$	(0.2857/0.01)

Table 2: System settings.

the use of α_{ref} and $\bar{\alpha}$ are thereby compared with the conventional case, where only the Wiener filter is applied to both the low band and the high band, and the BWE supported wideband noise suppression system using MFCC features with α_{ref} [1]. The parameters that have been used in the simulations are listed in Tab. 2. The look-up tables which are required for the estimation of α_{ref} were generated based on 10 min of clean speech from the NTT database disturbed by white Gaussian noise at different input SNR values.

In the simulation setup, the speech and noise signal can be filtered separately with weighting gains adapted for the noisy signal. Hence, the output signal can additionally be stated as $\hat{s}(k) = \tilde{s}(k) + \tilde{n}(k)$, where $\tilde{s}(k)$ is merely the filtered speech signal and $\tilde{n}(k)$ the filtered noise signal. Based on these quantities, the segmental speech SNR (SpSNR) and the segmental noise attenuation (NA) were calculated according to [15]. For the objective evaluation of the noise reduction schemes, seven speech signals from the NTT speech database were each degraded by four different noise types (cockpit, babble, factory1, buccaneer), taken from the NOISEX-92 database. Among the seven speech signals, there were four sequences from a male and three from a female speaker, each with a length of 8 seconds. The speech signals used for the evaluation were not included in the training data for the HMM and the look-up tables

Figure 3 depicts the averaged results for SpSNR plotted over NA with the input SNR as control variable. Thus, a fair comparison with respect to the tradeoff noise attenuation and speech distortion is possible. The points of best performance would be placed in the upper right corner of the figure.

The objective measurements show that the additional use of the artificial BWE in the high band improves the results of conventional noise suppression techniques consistently. The adaption of features and the training process for the HMM outperforms the Wiener filter as well as the BWE wideband noise suppression system using [1]. It can be seen that the performance for the proposed method using $\bar{\alpha}$ and α_{ref} are very similar. At low SNR values the proposed method benefits from the enhanced noisy training process, while the used RASTA-PLP features improve the SpSNR at higher SNR values. Informal listening tests confirmed the instrumental measurements and showed that the occurrence of *musical tones* is reduced by the proposed method.

5 Conclusions

An approach to wideband speech enhancement has been presented in this paper that exploits spectral dependencies of speech signals. In [1], it was shown that the enhanced low band signal can be re-used to improve the results of a conventional noise suppression technique in the high band based on a artificial bandwidth extension. As novel feature



Figure 3: Segmental speech SNR vs. noise attenuation.

the training process is adapted to noisy speech in this paper. Therefore the training data is degraded by white Gaussian noise and afterwards enhanced for the HMM training process. In addition, the used RASTA-PLP features are more robust against short-term noise variations compared to MFCC features and minimize the speaker difference. In order to increase the perceived speech quality if only a noisy low band signal has been received, a slightly modified version of the system can additionally be used to perform a joint noise reduction and BWE.

References

- T. Esch, F. Heese, B. Geiser, and P. Vary, "Wideband noise suppression supported by artificial bandwidth extension techniques," in *Proc. of ICASSP*, Dallas, TX, USA, Mar. 2010.
- [2] 3GPP TS 26.171, "AMR wideband speech codec; general description," Mar. 2001.
- [3] J. S. Lim and A. V. Oppenheim, "Enhancement and Bandwidth Compression of Noisy Speech," *Proceedings of the IEEE*, 1979.
- [4] Y. Ephraim and D. Malah, "Speech Enhancement Using a Minimum Mean-Square Error Short-Time Spectral Amplitude Estimator, *IEEE Transactions on Acoustic, Speech and Signal Processing*, vol. 32, no. 6, pp. 1109–1121, 1984.
- [5] T. Lotter and P. Vary, Speech Enhancement by MAP Spectral Amplitude Estimation using a Super-Gaussian Speech Model," *EURASIP Journal on Applied Signal Proc.*, 2005.
- [6] B. Geiser, H. Taddei, and P. Vary, "Artificial Bandwidth Extension without Side Information for ITU-T G.729.1," in *Proc. of INTER-SPEECH*, Antwerp, Belgium, Aug. 2007.
- [7] P. Jax and P. Vary, "Bandwidth Extension of Speech Signals: A Catalyst for the Introduction of Wideband Speech Coding?," in *Communications Magazine, IEEE*, May 2006, vol. 44.
- [8] H. W. Löllmann, M. Hildenbrand, B. Geiser, and P. Vary, "IIR QMF-bank design for speech and audio subband coding," in *Proc.* of *IEEE Workshop on Applications of Signal Processing to Audio* and Acoustics (WASPAA), New Paltz, NY, USA, Oct. 2009.
- [9] C. Beaugeant, M. Schönle, and I. Varga, "Challenges of 16 kHz in Acoustic Pre- and Post-Processing for Terminals," *IEEE Communications Magazine*, vol. 44, no. 5, pp. 98–104, May 2006.
- [10] R. Martin, "Noise Power Spectral Density Estimation Based on Optimal Smoothing and Minimum Statistics," *IEEE Transactions* on Speech and Audio Processing, vol. 9, no. 5, pp. 501–512, 2001.
- [11] P. Jax and P. Vary, "Feature Selection for Improved Bandwidth Extension of Speech Signals,"in *Proc. of ICASSP*, Montreal, Canada, May 2004.
- [12] H. Hermansky and N. Morgan, "RASTA processing of speech," *IEEE transactions on speech and audio processing*, vol. 2, no. 4, pp. 578–589, 1994.
- [13] H. Hermansky, "Perceptual linear predictive (PLP) analysis of speech," *Journal of the Acoustical Society of America*, vol. 87, no. 4, 1990.
- [14] Y. Linde, A. Buzo, and R. Gray, "An Algorithm for Vector Quantizer Design," *IEEE Trans. on Communications*, vol. 28, no. 1, 1980.
- [15] S. Gustafsson, R. Martin, P. Jax, and P. Vary, "A Psychoacoustic Approach to Combined Acoustic Echo Cancellation and Noise Reduction," *IEEE Trans. on Speech and Audio Processing*, 2002.